



West Ridge of Mt. Everest

# Viscosity and the Soft Ridge at RHIC

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Ridge in 2-particle correlations with **no** jet tag  
Claim: viscous hydro can explain this!

I. Soft ridge (no jet tag)

SG + Abdel-Aziz, PRL  
97, 162302 (2006)

II. Transverse flow fluctuations in viscous hydro

III. Effect on transverse momentum correlations

SG + G. Moschelli,  
in progress

IV. Rapidity + Azimuthal Correlation Data

V. Implications for "hard ridge"

Pruneau, Voloshin +  
SG, NPA, in press



# Momentum Correlation Landscape

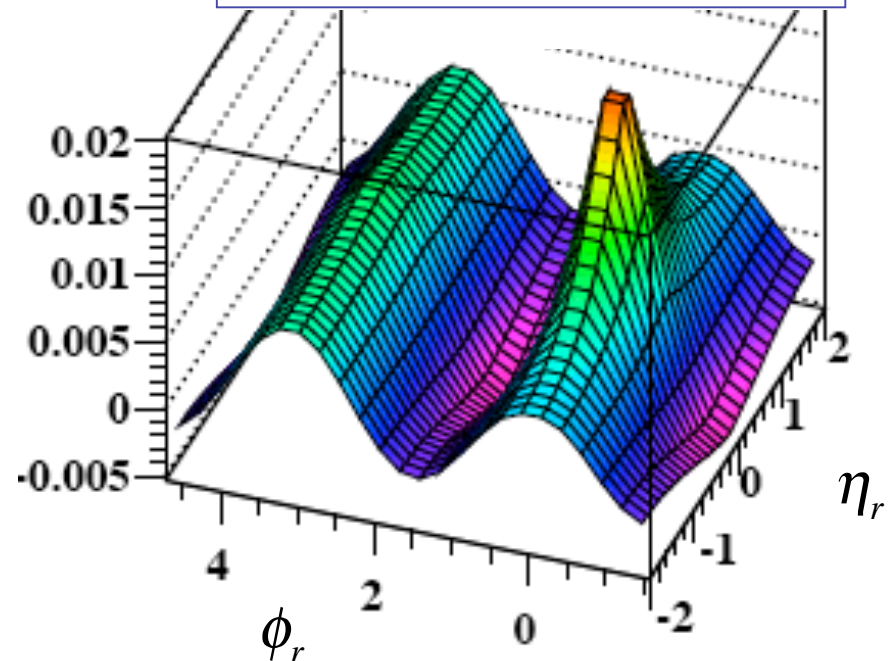
**soft ridge:** near side peak

similar to **ridge** with jet tag

**but** at ordinary  $p_t$  scales

-- no jet tag

STAR, J.Phys. G32 (2006) L37



**STAR  $p_t$  fluctuations**

$$\Delta\sigma_{p_t:n} = \frac{1}{\langle N \rangle} \left\langle \sum_{pairs} (p_{ti} - \langle p_t \rangle)(p_{tj} - \langle p_t \rangle) \right\rangle \longrightarrow \int (\text{correlation function}) d\eta_r d\phi_r$$

**jet-like correlations from flow** -- Voloshin; Shuryak

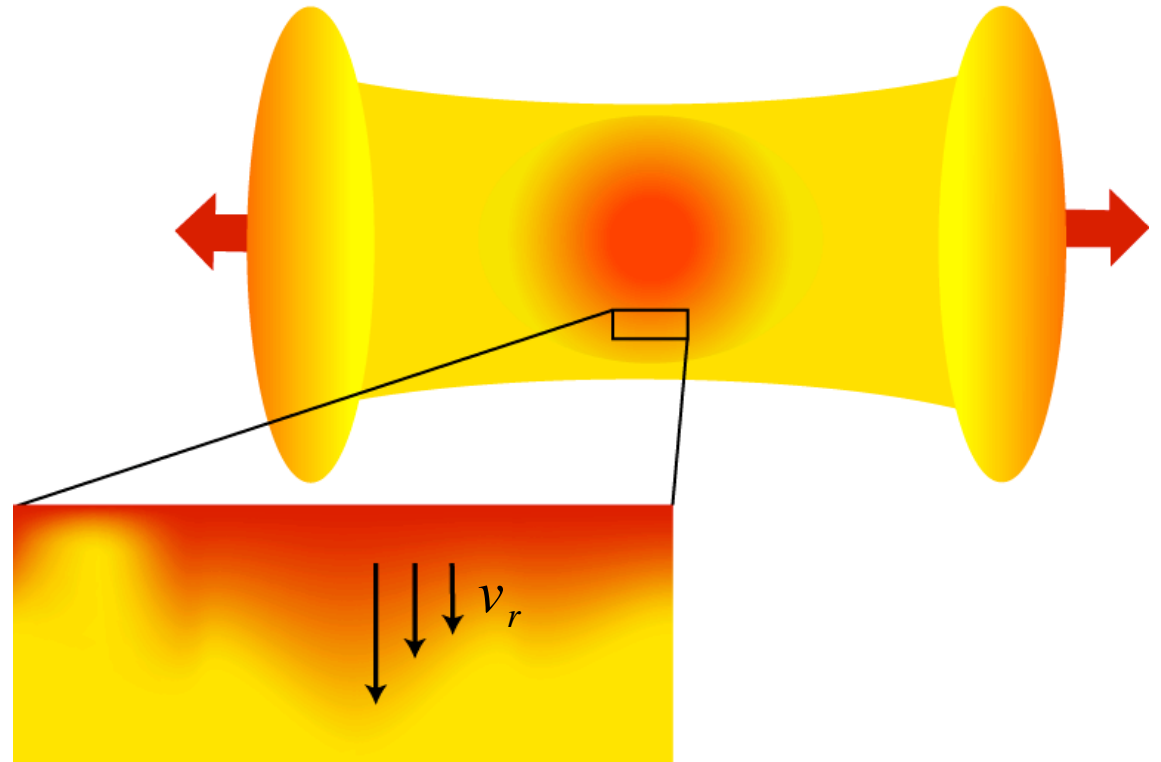
**our aim:** hydro explanation for untagged correlations

# Transverse Flow $\rightarrow p_t$ Fluctuations

small variations in radial flow  
in each event

neighboring fluid elements  
flow past one another  
 $\Rightarrow$  viscous friction

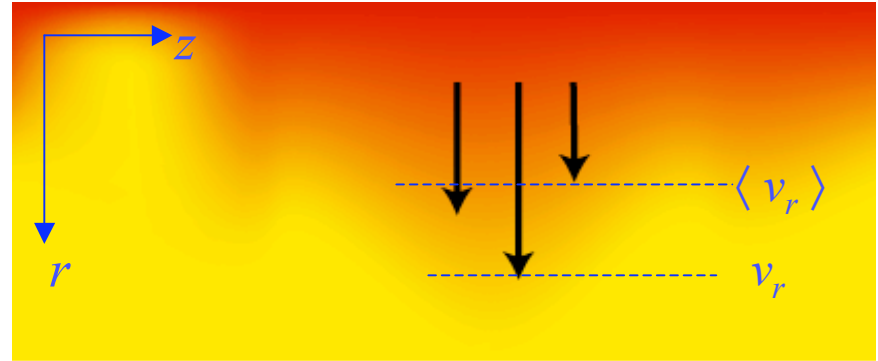
**shear viscosity drives  
velocity toward the  
average**



**motivation:** damping of radial flow fluctuations  $\Rightarrow$  viscosity



# Evolution of Fluctuations



## momentum current

small fluctuations

$$g_t \equiv T_{0r} - \langle T_{0r} \rangle$$

**diffusion equation** for  
momentum current

$$\frac{\partial}{\partial t} g_t = \frac{\eta}{sT} \nabla^2 (g_t + \text{noise})$$

shear viscosity  $\eta$ , entropy density  $s$ , temperature  $T$   
fluctuations  $\rightarrow$  Langevin noise

**diffusion +  
transverse flow**

$$\frac{\partial g_t}{\partial \tau} + \langle \vec{v}_r \rangle \cdot \vec{\nabla}_t g_t + g_t \frac{\partial \langle v_r \rangle}{\partial r} = \frac{\eta}{sT} \nabla^2 (g_t + \text{noise}), \quad v_r \ll 1$$

# Hydrodynamic Momentum Correlations

SG + Abdel-Aziz, PRL 97, 162302 (2006)

## momentum flux density correlation function

$$r_g = \langle g_t(x_1)g_t(x_2) \rangle - \langle g_t(x_1) \rangle \langle g_t(x_2) \rangle$$

$\Delta r_g = r_g - r_{g,eq}$  satisfies diffusion equation (no noise)

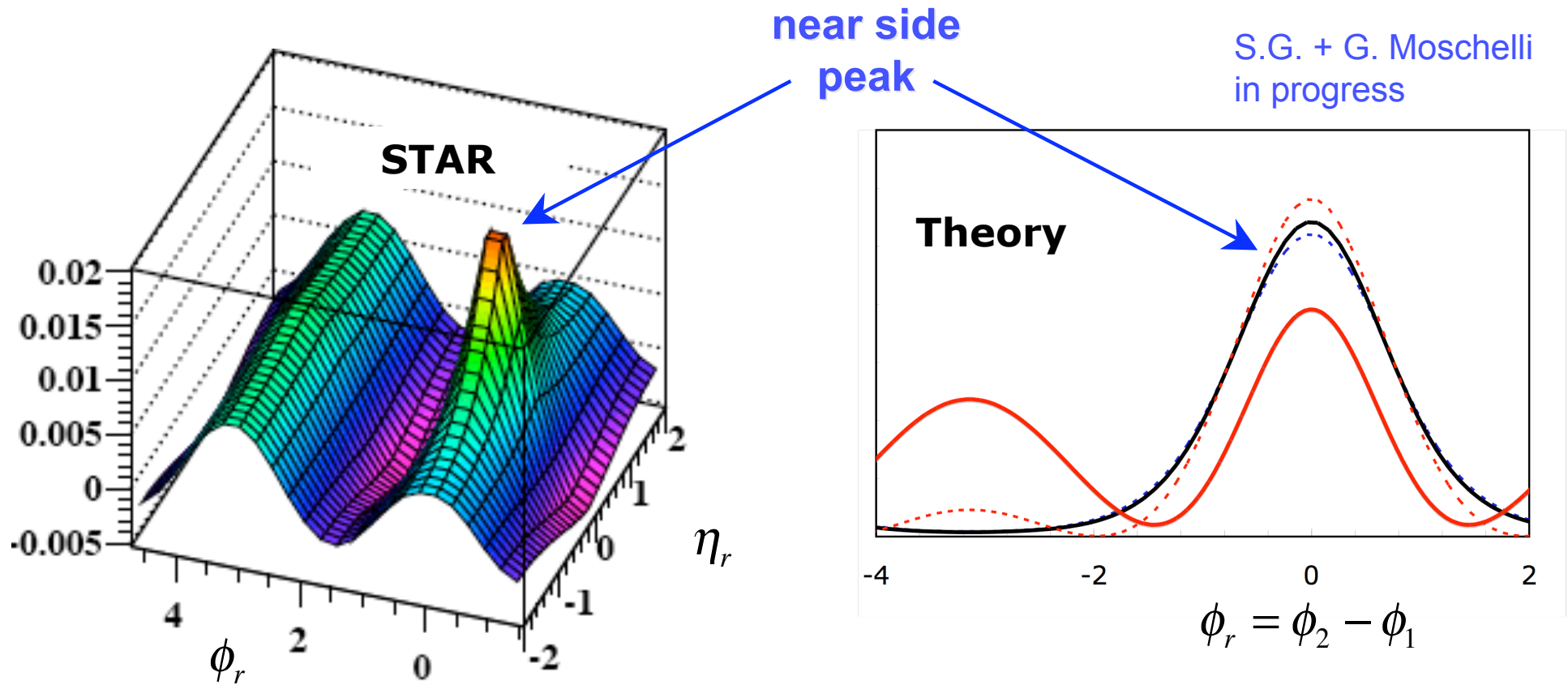
**observable:**

$$C = \frac{1}{\langle N \rangle^2} \left\langle \sum_{\text{pairs}} p_{ti} p_{tj} \right\rangle - \langle p_t \rangle^2 = \frac{1}{\langle N \rangle^2} \int \Delta r_g dp_1 dp_2$$

**STAR measured:**

$$\begin{aligned} \Delta \sigma_{p_t:n} &= \frac{1}{\langle N \rangle} \left\langle \sum_{i \neq j} (p_{ti} - \langle p_t \rangle)(p_{tj} - \langle p_t \rangle) \right\rangle \\ &= \langle N \rangle C - \langle p_t \rangle^2 \text{ (multiplicity fluctuations)} \end{aligned}$$

# Momentum Correlation Landscape



# Soft Ridge: Centrality Dependence

## near side peak

- pseudorapidity width  $\sigma \rightarrow \sigma_\eta$
- azimuthal width  $\sigma_\phi$

centrality dependence:

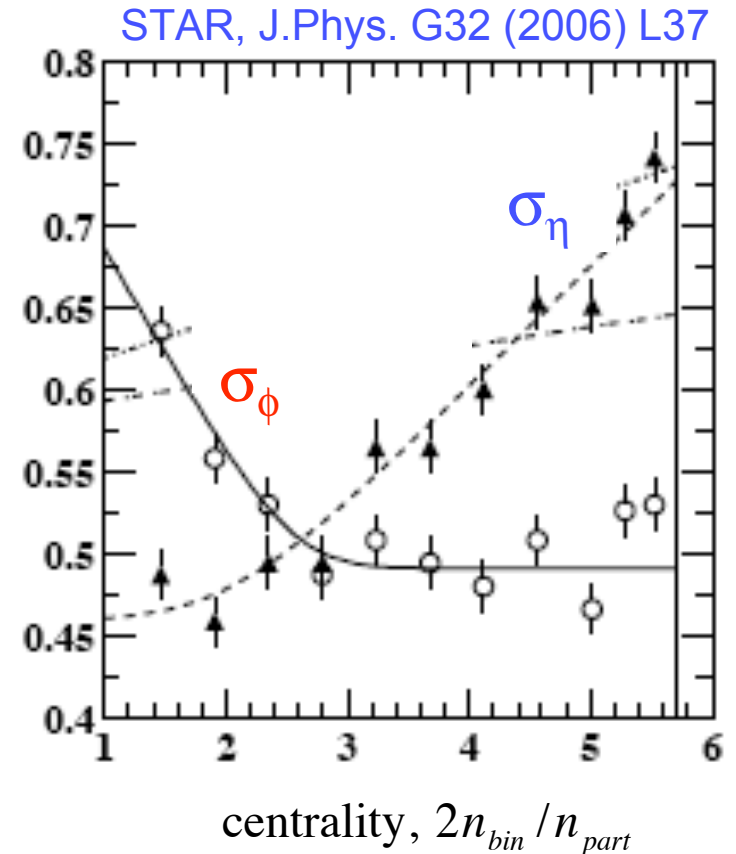
path length  $\sim 2n_{bin}/n_{part}$

## rapidity broadening:

viscous diffusion  $\Rightarrow 1/4\pi < \eta/s < 0.32$

SG + Abdel-Aziz, PRL 97, 162302 (2006)

**azimuthal narrowing:** viscous diffusion + transverse and elliptic flow





# Flow $\Rightarrow$ Azimuthal Correlations

**mean flow depends on position**

blast wave  $\vec{v}_r \sim \lambda \vec{r}$

**opening angle** for each fluid element depends on  $r$

$$\Delta\phi \sim v_{th}/v_r \sim (\lambda r)^{-1}$$

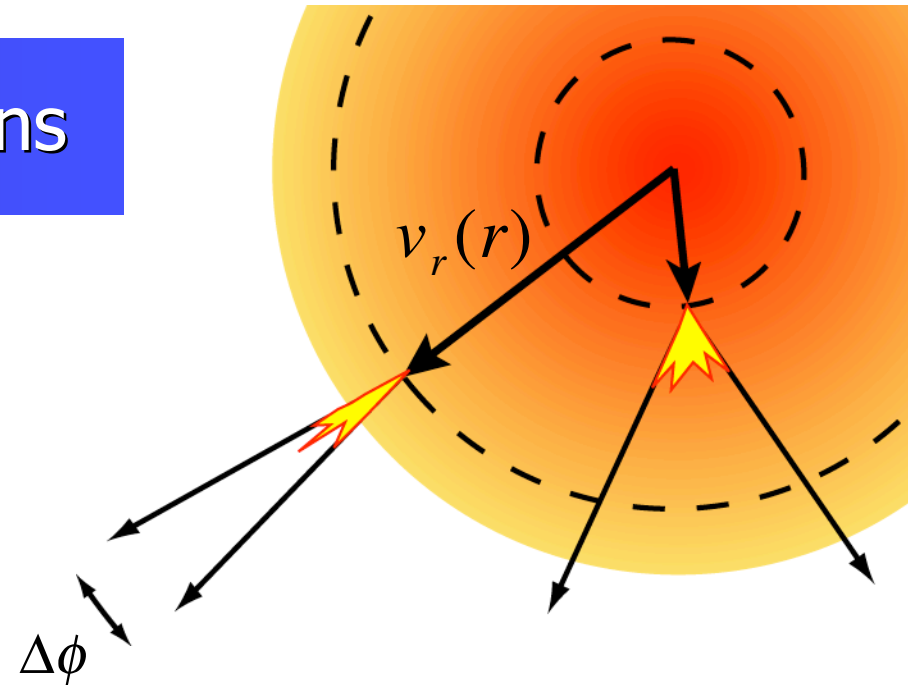
**correlations:**

gaussian spatial  $r(x_1, x_2)$ :

- $\sigma_t$  -- width in  $\vec{r} = \vec{r}_{t2} - \vec{r}_{t1}$
- $\Sigma_t$  -- width in  $\vec{R} = (\vec{r}_{t1} + \vec{r}_{t2})/2$

momentum distribution:

$$f = e^{-\gamma(E - \vec{p} \cdot \vec{v})/T}$$



$$\Delta r_g(p_1, p_2) = \iint_{x_1, x_2} f(p_1, x_1) f(p_2, x_2) \Delta r_g(x_1, x_2)$$

$\Rightarrow$

$$\sigma_\phi^2 = \langle \Delta\phi^2 \rangle \propto \lambda^{-2} (\Sigma_t^2 - \sigma_t^2 / 4)^{-1}$$

# Measured Flow Constrains Correlations

## diffusion + flow for correlations

$$\frac{\partial g_t}{\partial \tau} + \vec{v}_r \cdot \vec{\nabla}_t g_t + g_t \frac{\partial v_t}{\partial r} = \frac{\eta}{sT} \nabla^2 g_t \longrightarrow \Sigma_t(\tau), \sigma_t(\tau)$$

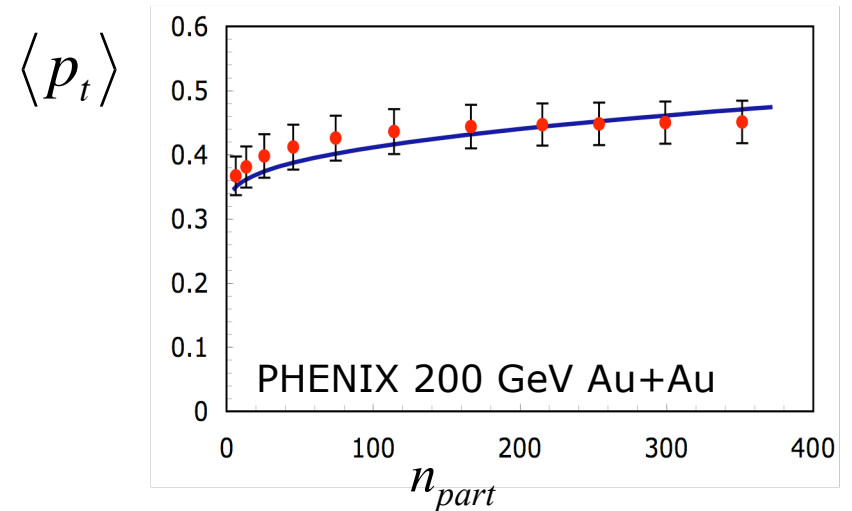
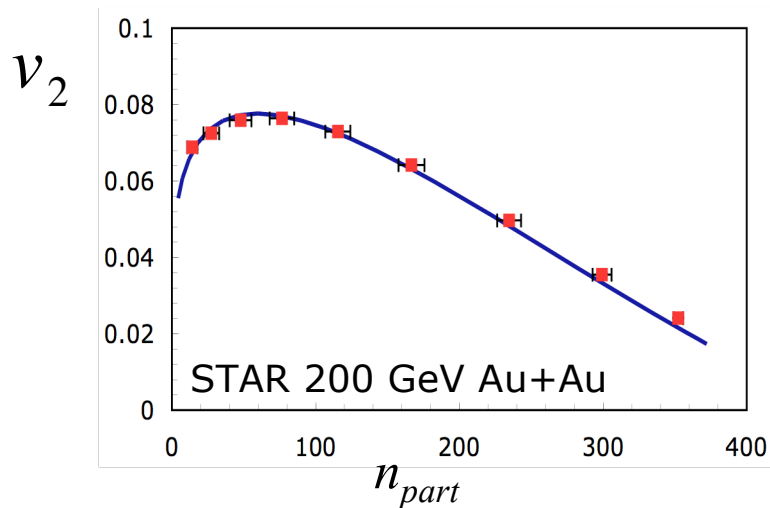
## radial plus elliptic flow:

"eccentric" blast wave

Heinz et al.

$$\vec{v}_r = \varepsilon_x(\tau) x \hat{x} + \varepsilon_y(\tau) y \hat{y}$$

**constraints:** flow velocity, radius from measured  $v_2, \langle p_t \rangle$  vs. centrality



# Rapidity and Azimuthal Trends

G. Moschelli + S.G., *in progress*

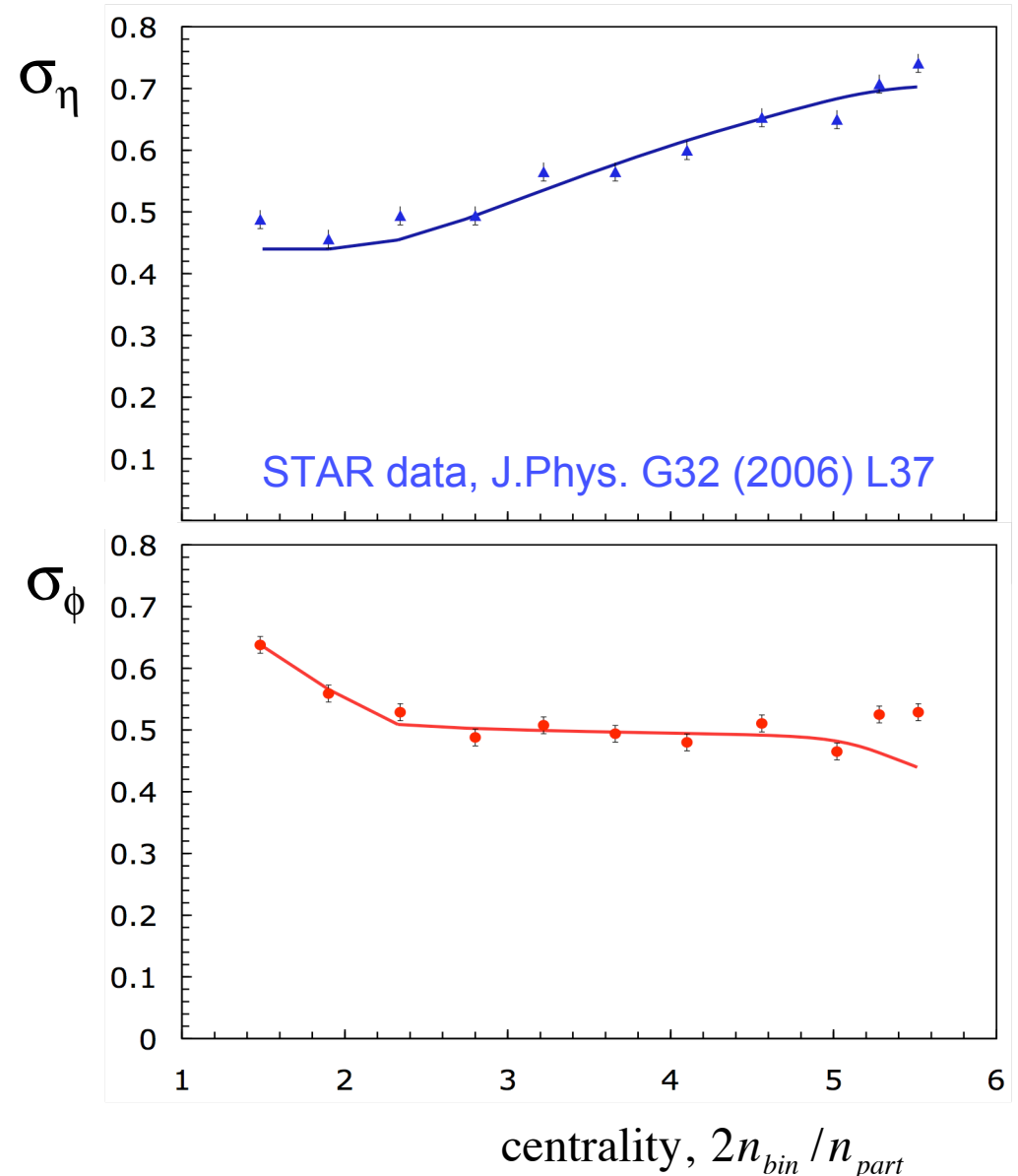
## rapidity width:

- viscous broadening,  $\eta/s \sim 1/4\pi$
- assume local equilibrium for all impact parameters

## azimuthal width:

- flow dominates
- viscosity effect tiny

agreement with data easier if  
we ignore peripheral region  
-- nonequilibrium?



# Summary: what can we learn from the soft ridge?

## viscous hydro can explain two-particle correlations

- azimuthal and rapidity correlations **explained**
- **very small**  $\eta/s \sim 1/4\pi$

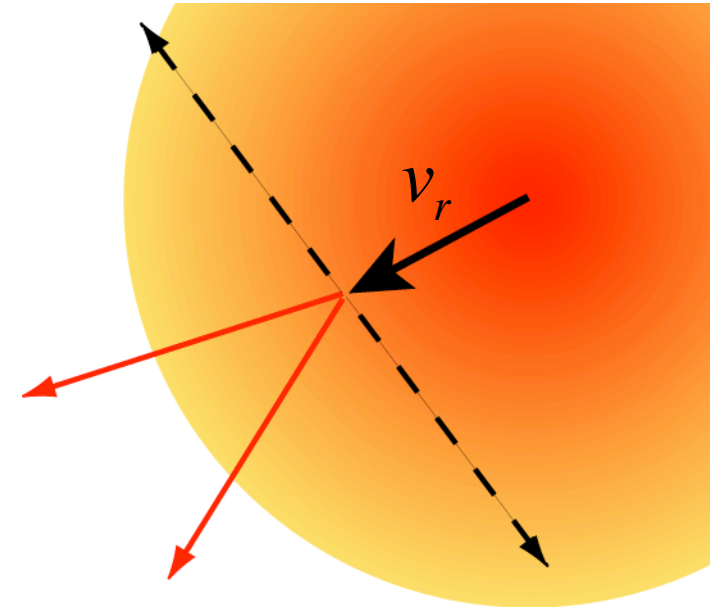
## does the jet cause the jet-tag ridge?

- **soft ridge:** ridge-like feature without jet tag
- **correlation:** jet tag and transversely-expanding fluid both fly outward
- **correlation  $\neq$  causation**

# Hard Ridge: Transverse Flow?

any effect of transverse flow on jets  $\Rightarrow$  ridge-like structure

C. Pruneau, S. Voloshin + S.G.,  
Nucl Phys A to be published



## PYTHIA + transverse boost

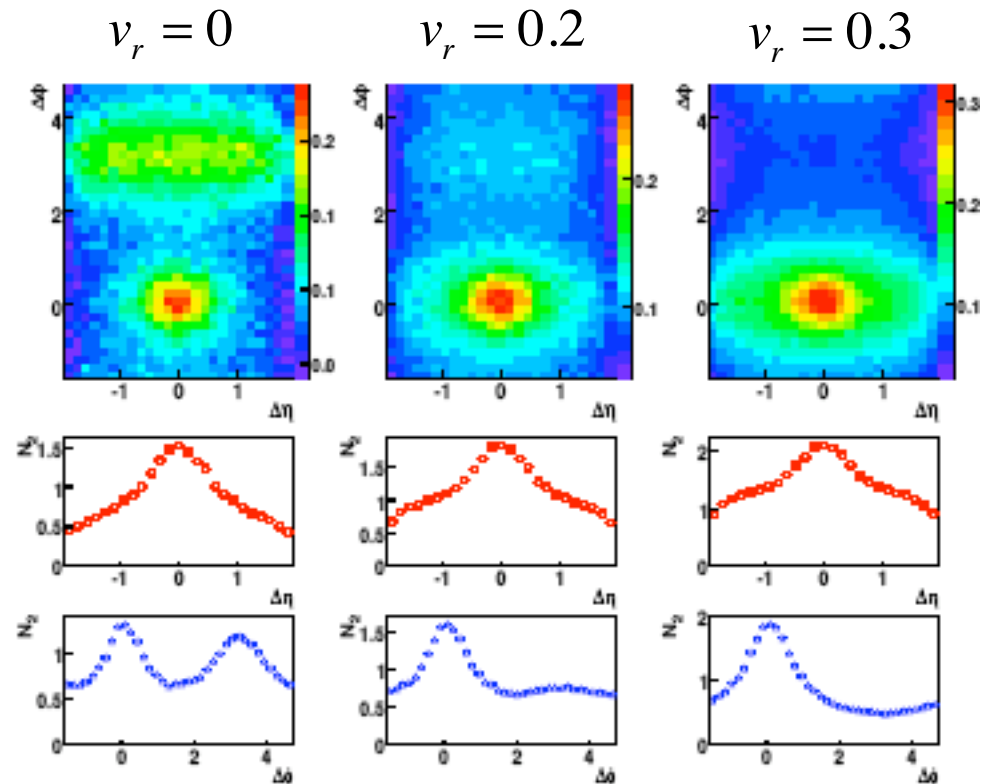
- jet tag particle  $3 < p_t < 20$  GeV
- associates  $0.2 < p_t < 1$  GeV

## flow-like effects for jets?

- Cronin (pA, dA, leptons)
- radial color fields

Fries, Kapusta + Li

**further clues from 3 particle correlations**



# Azimuthal Correlations from Flow

**transverse flow:** narrows angular correlations

- no flow  $\Rightarrow \sigma_\phi = \pi/\sqrt{3}$
- $\sigma_\phi \propto 1/v_{rel}$

**elliptic flow:**

- $v_2$  contribution
- STAR subtracted

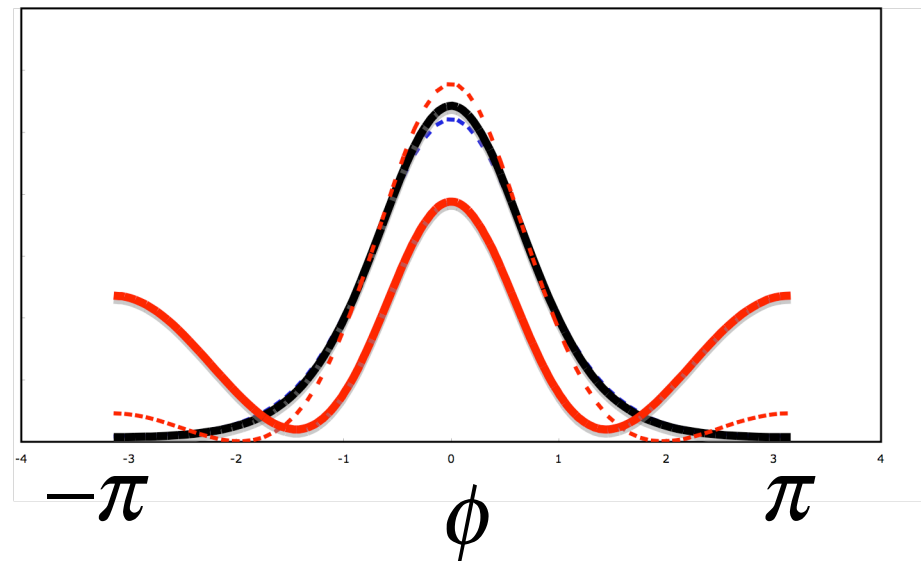
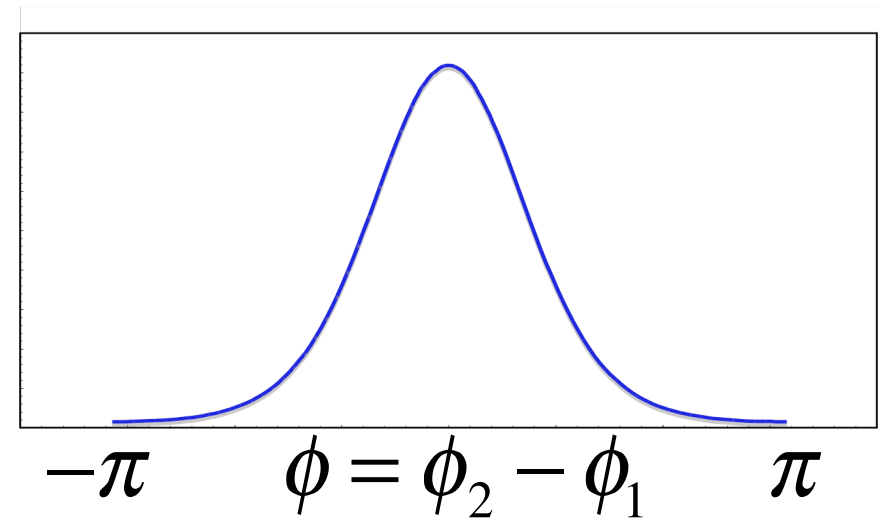
**momentum conservation:**

- $\propto \sin \phi$  ; subtracted

Borghini, et al

**viscous diffusion:**

- increases spatial widths  $\Sigma_t$  and  $\sigma_t$
- $\sigma_\phi \propto (\Sigma_t^2 - \sigma_t^2/4)^{-1/2}$





# Uncertainty Range

we want:

$$C = \frac{1}{\langle N \rangle^2} \left\langle \sum_{i \neq j} p_{ti} p_{tj} \right\rangle - \langle p_t \rangle^2$$

STAR measures:  $\langle N \rangle \Delta \sigma_{p_t:n} = \left\langle \sum_{i \neq j} (p_{ti} - \langle p_t \rangle) (p_{tj} - \langle p_t \rangle) \right\rangle$

$$= \int dx_1 dx_2 \left[ \Delta r_g(x_1, x_2) - \langle p_t \rangle^2 \Delta r_n(x_1, x_2) \right]$$

momentum density correlations

density correlations

## density correlation function

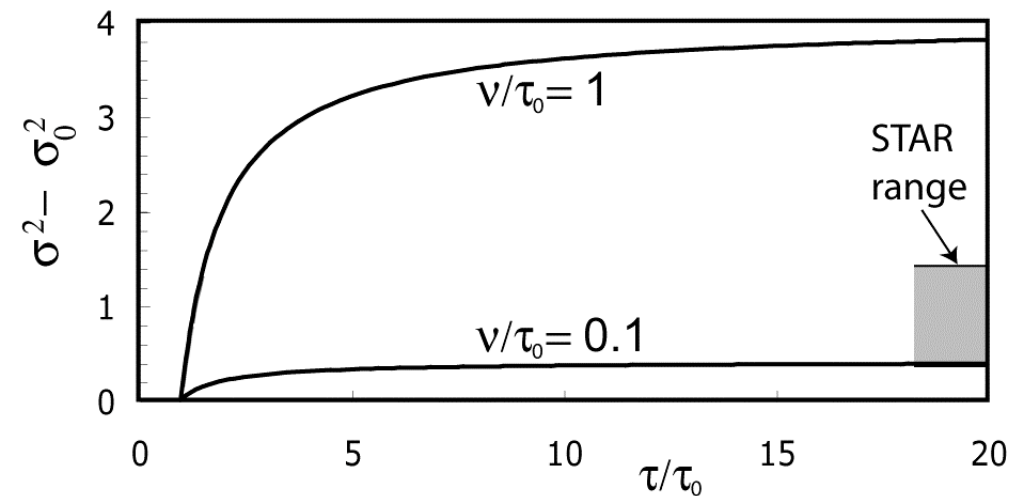
$\Delta r_n = r_n - r_{n,eq}$  may differ from  $\Delta r_g$

maybe  $\sigma_n \approx 2\sigma_*$

STAR, PRC 66, 044904 (2006)

uncertainty range  $\sigma_* \leq \sigma \leq 2\sigma_*$

$\Rightarrow 0.08 \leq \eta/s \leq 0.3$



# Covariance $\Rightarrow$ Momentum Flux

covariance  $C = \frac{1}{\langle N \rangle^2} \left\langle \sum_{\text{pairs } i \neq j} p_{ti} p_{tj} \right\rangle - \langle p_t \rangle^2$

unrestricted sum:  $\sum_{\text{all } i, j} p_{ti} p_{tj} = \int p_{t1} p_{t2} dn_1 dn_2$

$$\begin{aligned}
 & \left. \begin{aligned} dn &= f(x, p) dp dx \\ g_t(x) &= \int dp p_t \Delta f(x, p) \end{aligned} \right\} \\
 & \qquad \qquad \qquad = \int dx_1 dx_2 \left( \int dp_1 p_{t1} f_1 \right) \left( \int dp_2 p_{t2} f_2 \right) \\
 & \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \rightarrow \int g(x_1) g(x_2) dx_1 dx_2
 \end{aligned}$$

correlation function:  $r_g = \langle g_t(x_1) g_t(x_2) \rangle - \langle g_t(x_1) \rangle \langle g_t(x_2) \rangle$

$$\int r_g dx_1 dx_2 = \left\langle \sum p_{ti} p_{tj} \right\rangle - \langle N \rangle^2 \langle p_t \rangle^2 = \left\langle \sum p_{ti}^2 \right\rangle + \langle N \rangle^2 C$$

$C = 0$  in equilibrium  $\Rightarrow C = \frac{1}{\langle N \rangle^2} \int (r_g - r_{g,eq}) dx_1 dx_2$

# Current Data?

**STAR measures rapidity width of  $p_t$  fluctuations**

J.Phys. G32 (2006) L37

$$\Delta\sigma_{p_t:n} = \frac{1}{\langle N \rangle} \left\langle \sum_{i \neq j} (p_{ti} - \langle p_t \rangle)(p_{tj} - \langle p_t \rangle) \right\rangle$$

find width  $\sigma_*$  increases in central collisions

- most peripheral  $\sigma_* \sim 0.45$
- central  $\sigma_* \sim 0.75$

**naively identify**  $\sigma_*$  with  $\sigma$  (strictly,  $\Delta\sigma_{p_t:n} = \langle N \rangle C + \text{corrections}$ )

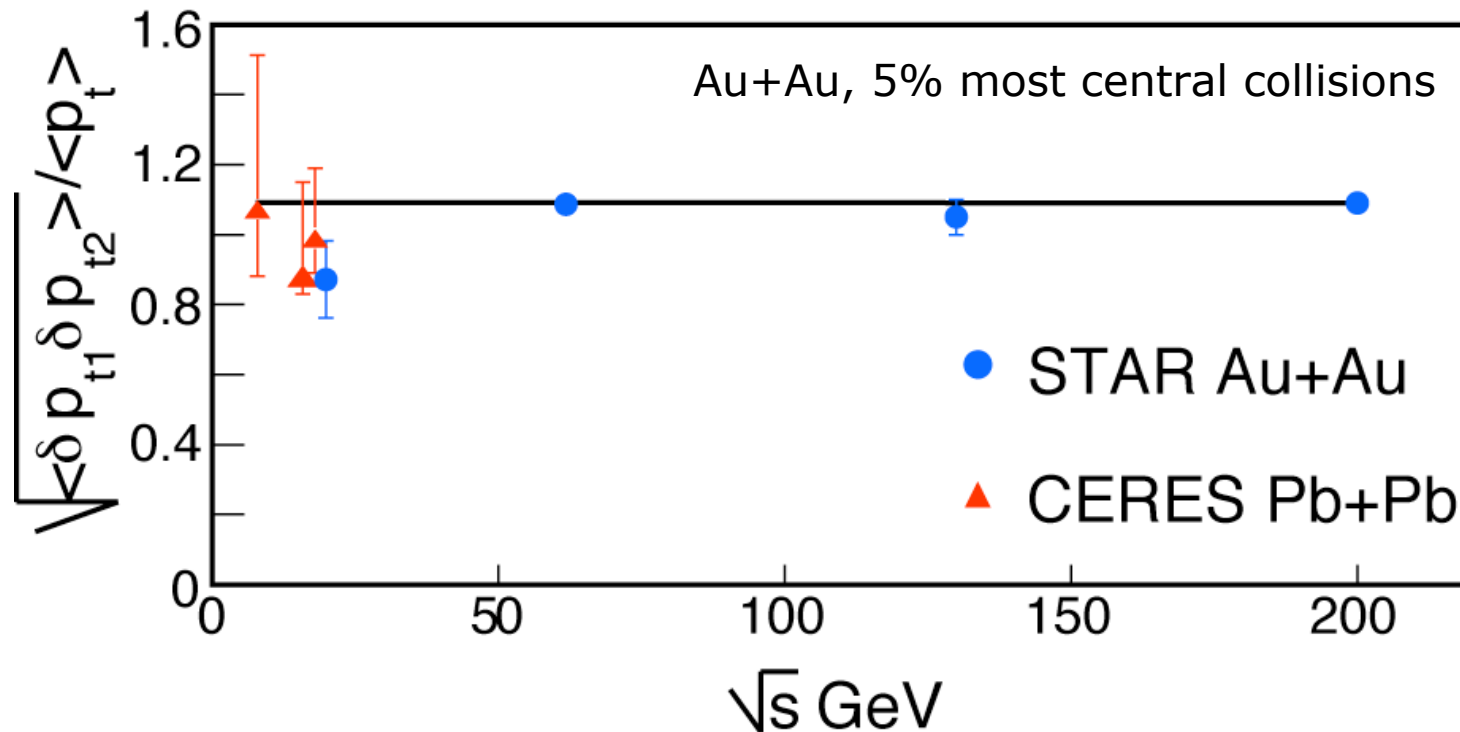
$$\sigma_{central}^2 - \sigma_{peripheral}^2 = 4v \left( \frac{1}{\tau_{f,p}} - \frac{1}{\tau_{f,c}} \right)$$

**but** maybe  $\sigma_n \approx 2\sigma_*$  STAR, PRC 66, 044904 (2006)

uncertainty range  $\sigma_* \leq \sigma \leq 2\sigma_* \Rightarrow$

$$0.08 < \eta/s < 0.3$$

# $p_t$ Fluctuations Energy Independent



sources of  $p_t$  fluctuations: thermalization, flow, jets?

- central collisions  $\Rightarrow$  thermalized
- energy independent bulk quantity  $\Rightarrow$  jet contribution small